# 44th Summer Symposium in Real Analysis

# Participant

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## Title of the talk

Descriptive complexity of Banach spaces

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#### Abstract

We introduce a new natural coding of separable Banach spaces. The set of codes consists of (pseudo)norms on a certain vector space and is equipped with a canonical Polish topology. We use this coding to investigate the descriptive complexities of some classical Banach spaces. Among other results, we show that  $\ell_2$  is

- (a) the unique (up to isometry) separable Banach space with a closed isometry class,
- (b) the unique (up to isomorphism) separable Banach space with an  $F_{\sigma}$  isomorphism class.